

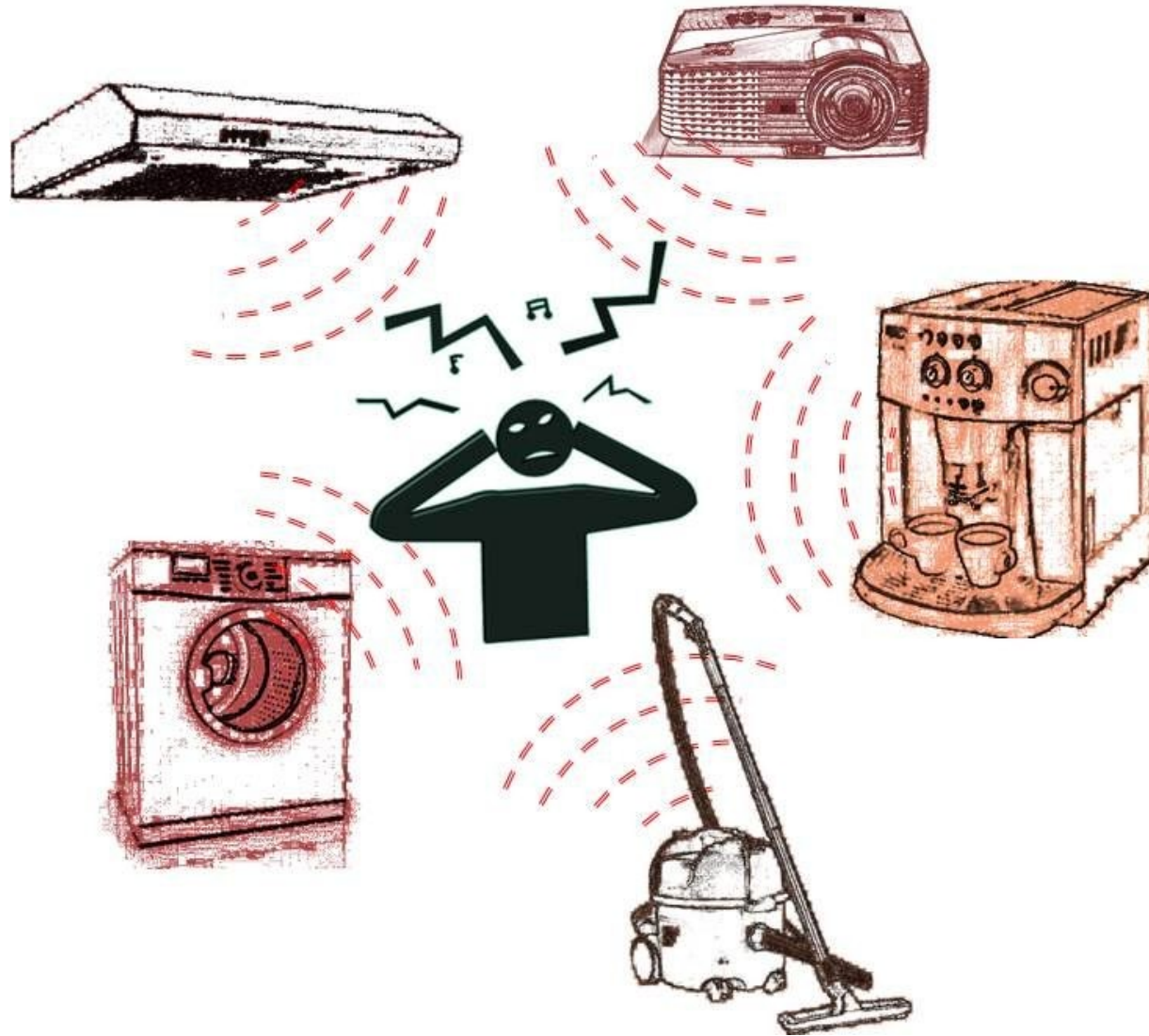
# Mechanical Vibrations

Prof. Paulo J. Paupitz Gonçalves

We are often subjected to  
vibration in our life



# We are often subjected to vibration problems in our life



# The importance of the study of Vibration



Figure 1.7

Tacoma Narrows bridge during wind-induced vibration. The bridge opened on July 1, 1940, and collapsed on November 7, 1940. (Farquharson photo, Historical Photography Collection, University of Washington Libraries).



# The importance of the study of Vibration

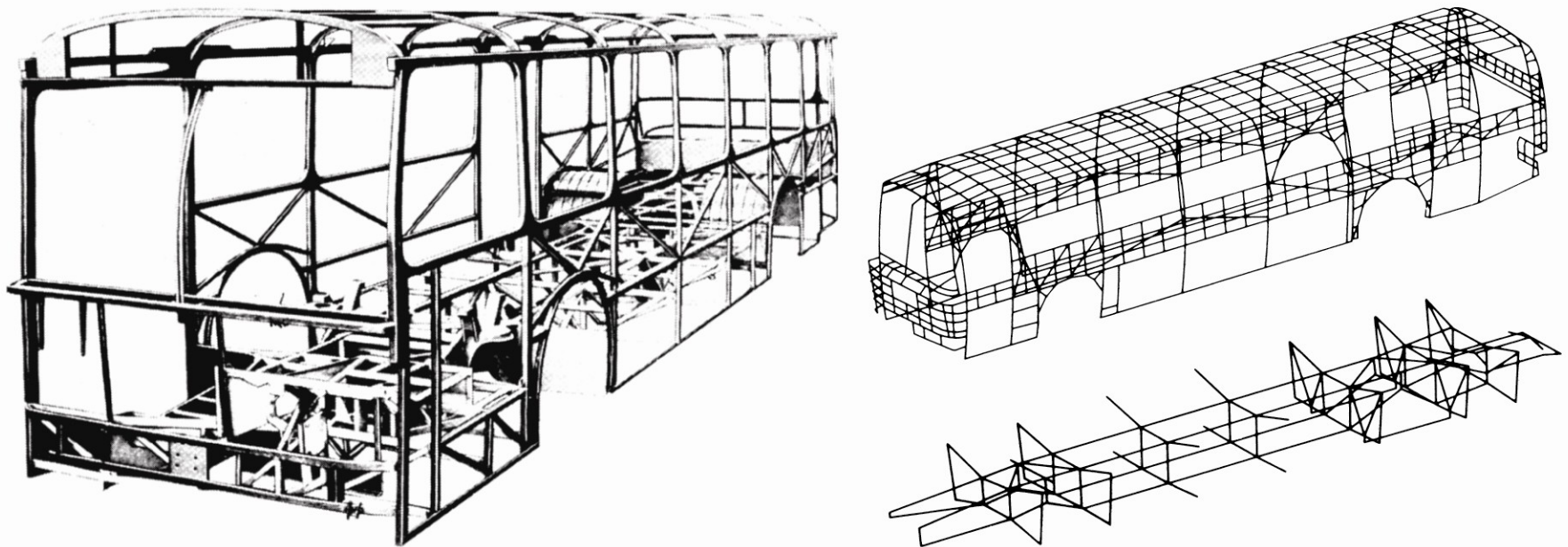
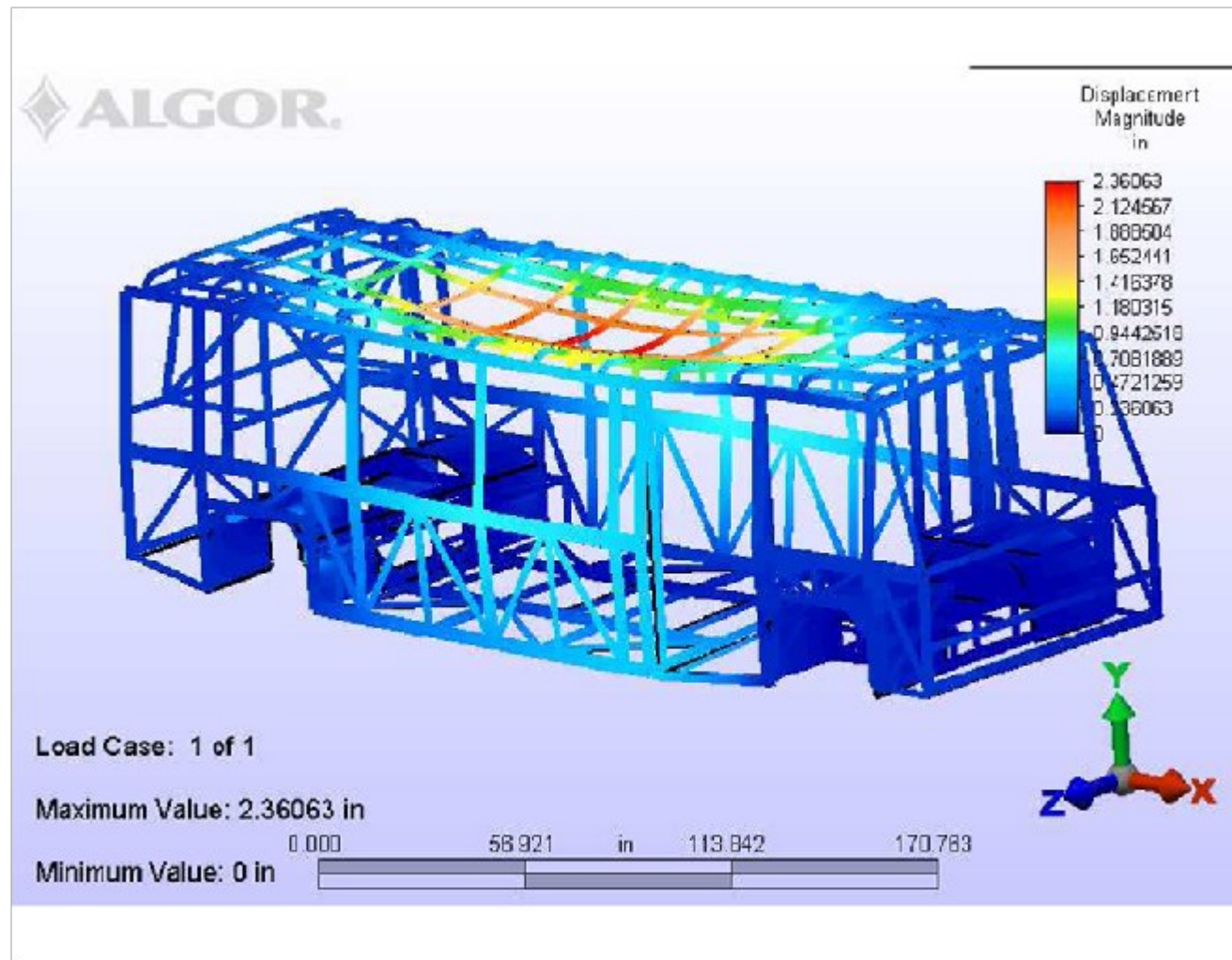


Figure 1.6

Finite element idealization of the body of a bus [1.16].  
(Reprinted with permission © 1974 Society of Automotive Engineers, Inc.)

# The importance of the study of Vibration



# The importance of the study of Vibration

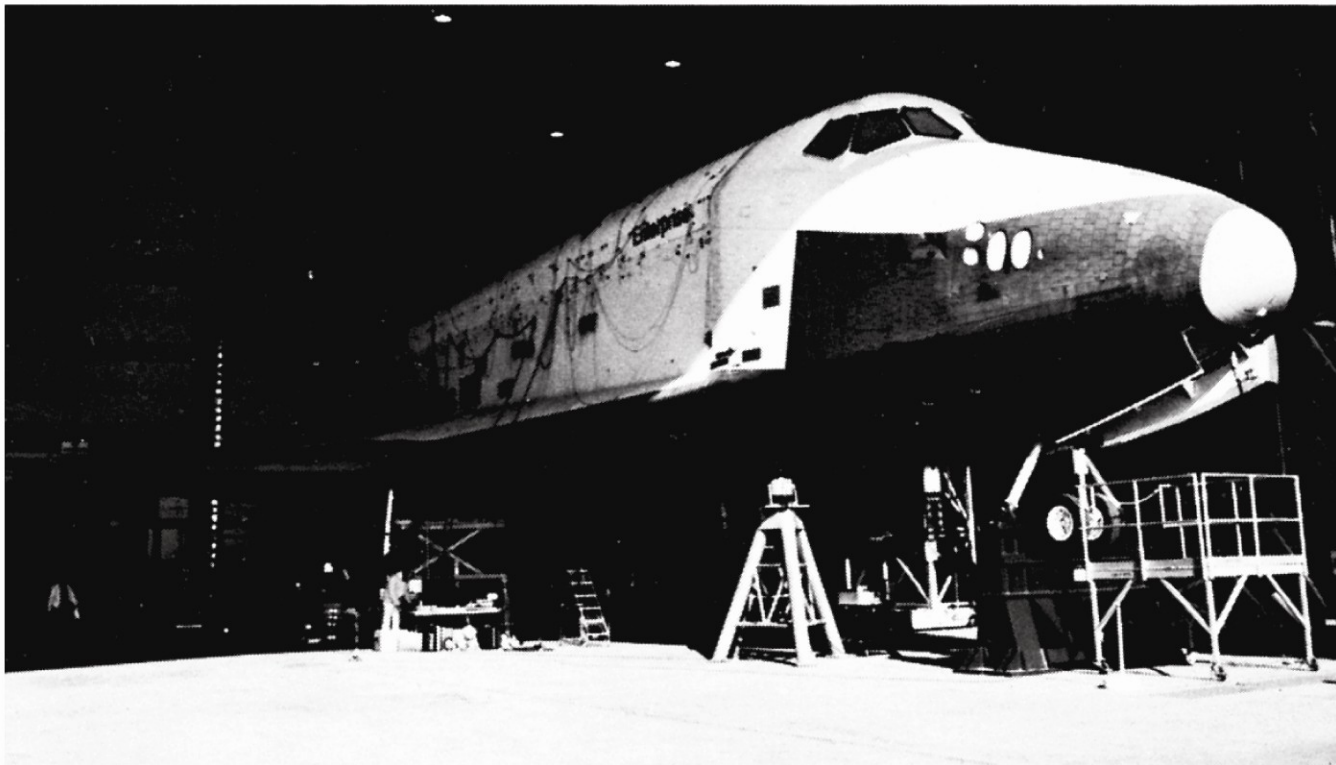


Figure 1.8

Vibration testing of the space shuttle *Enterprise*. (Courtesy of NASA).

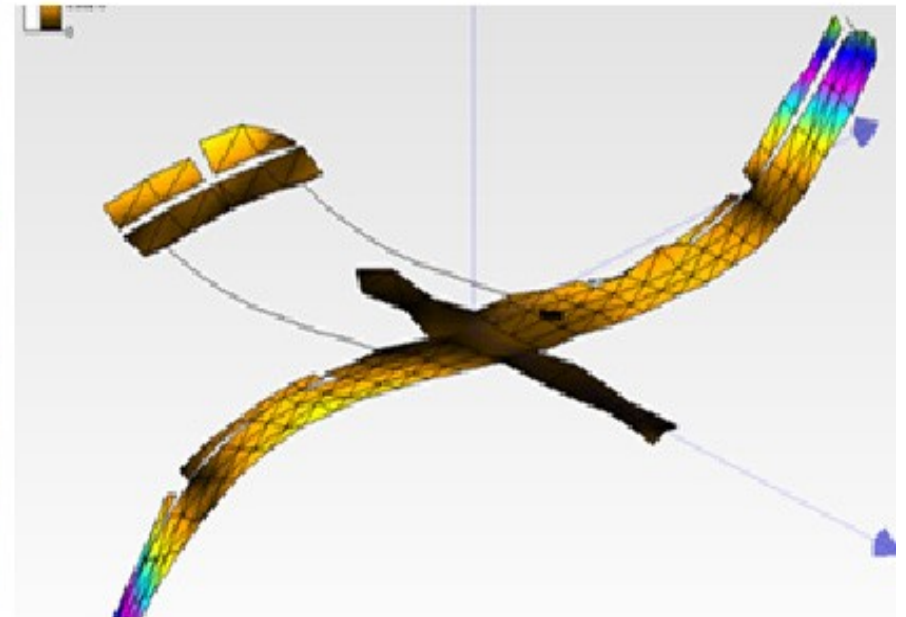


# The importance of the study of Vibration





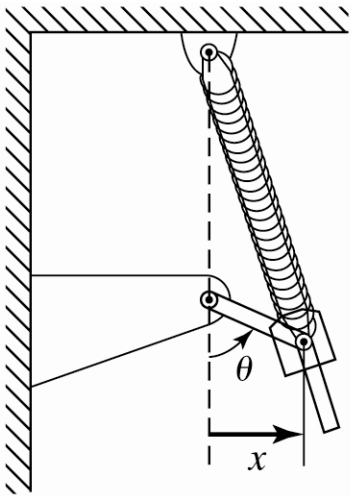
# The importance of the study of Vibration



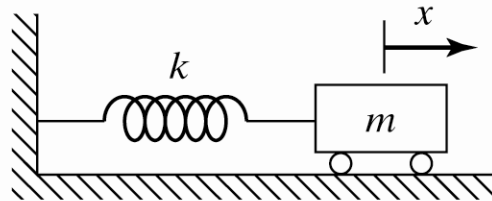
# Vibration Videos

# Basic Concepts

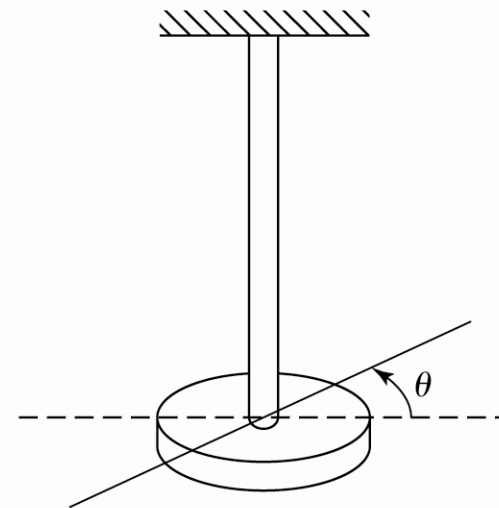
## Degrees of Freedom



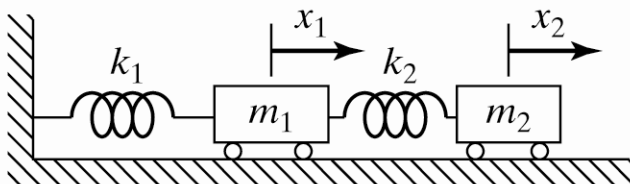
(a) Slider-crank-spring mechanism



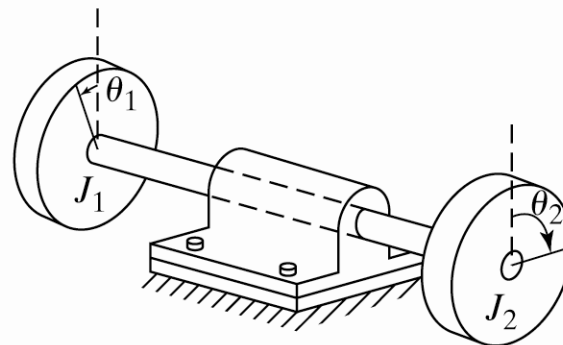
(b) Spring-mass system



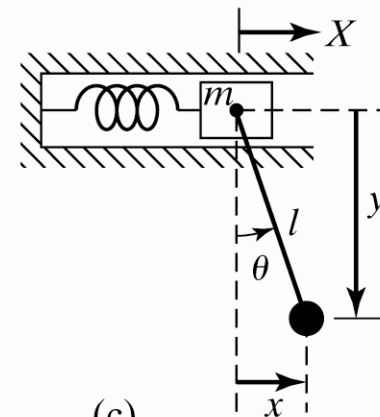
(c) Torsional system



(a)



(b)

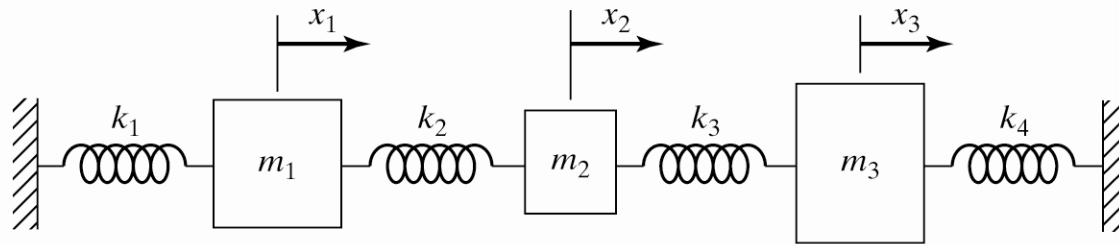


(c)

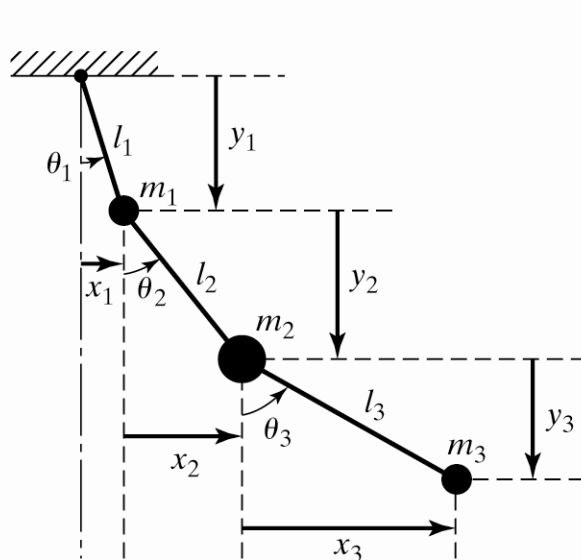


# Basic Concepts

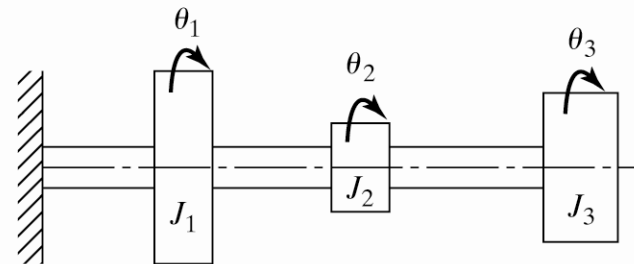
## Degrees of Freedom



(a)



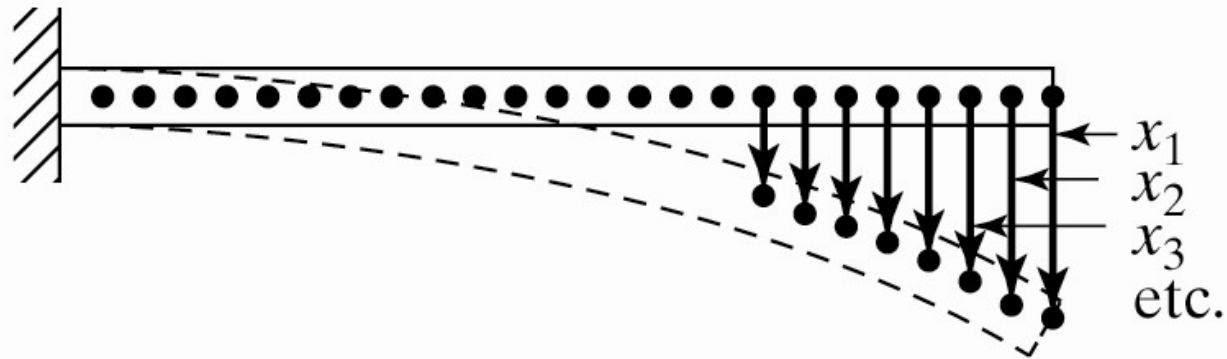
(b)



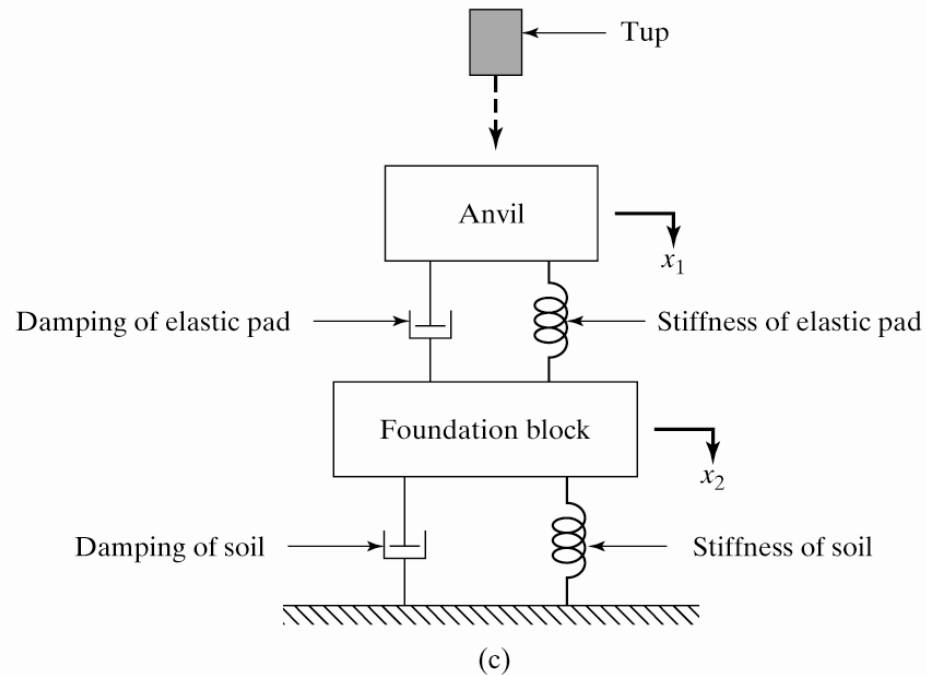
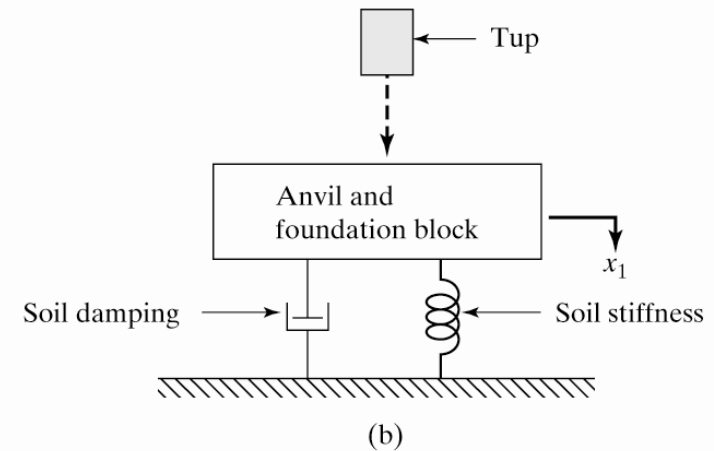
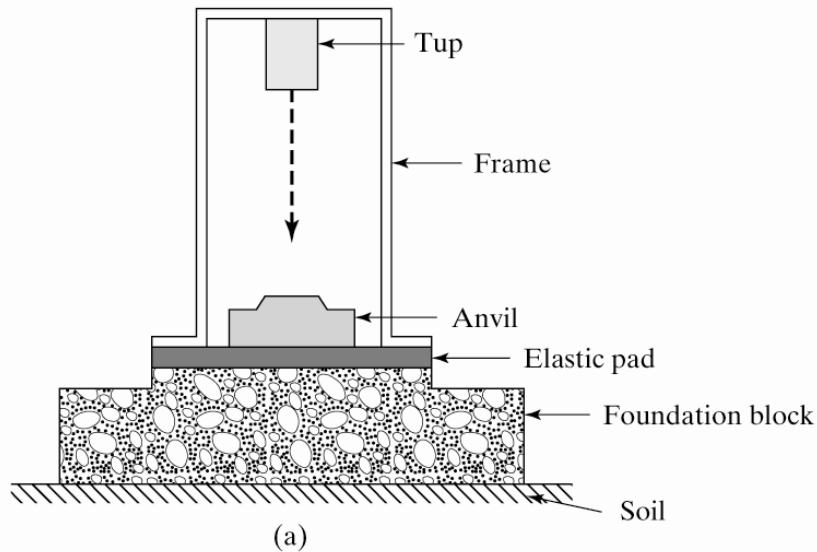
(c)

# Basic Concepts

## Degrees of Freedom

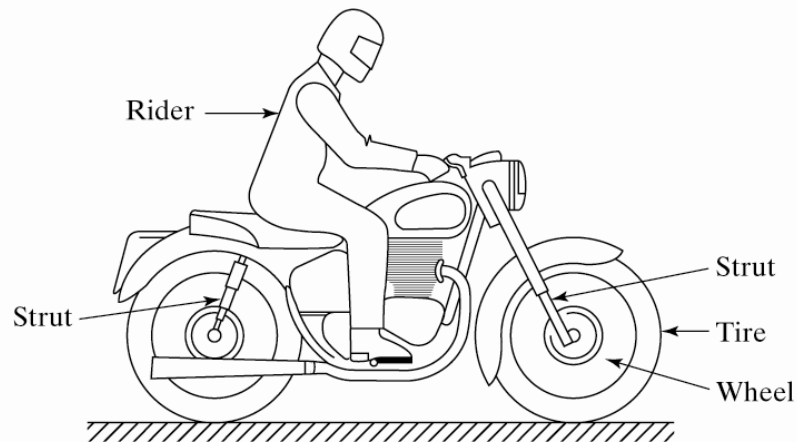


# Modelling of Mechanical Systems

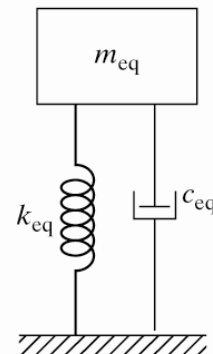




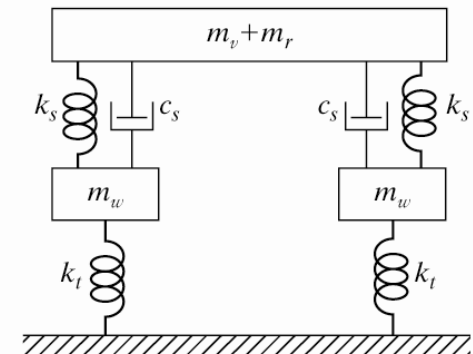
# Modelling of Mechanical Systems



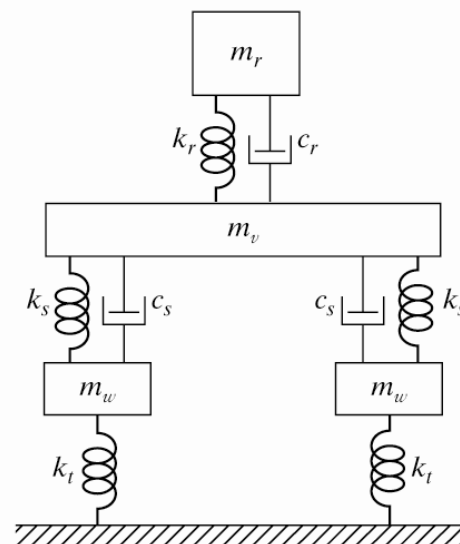
(a)



(b)

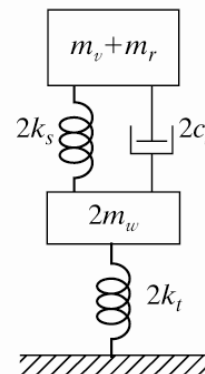


(c)



(d)

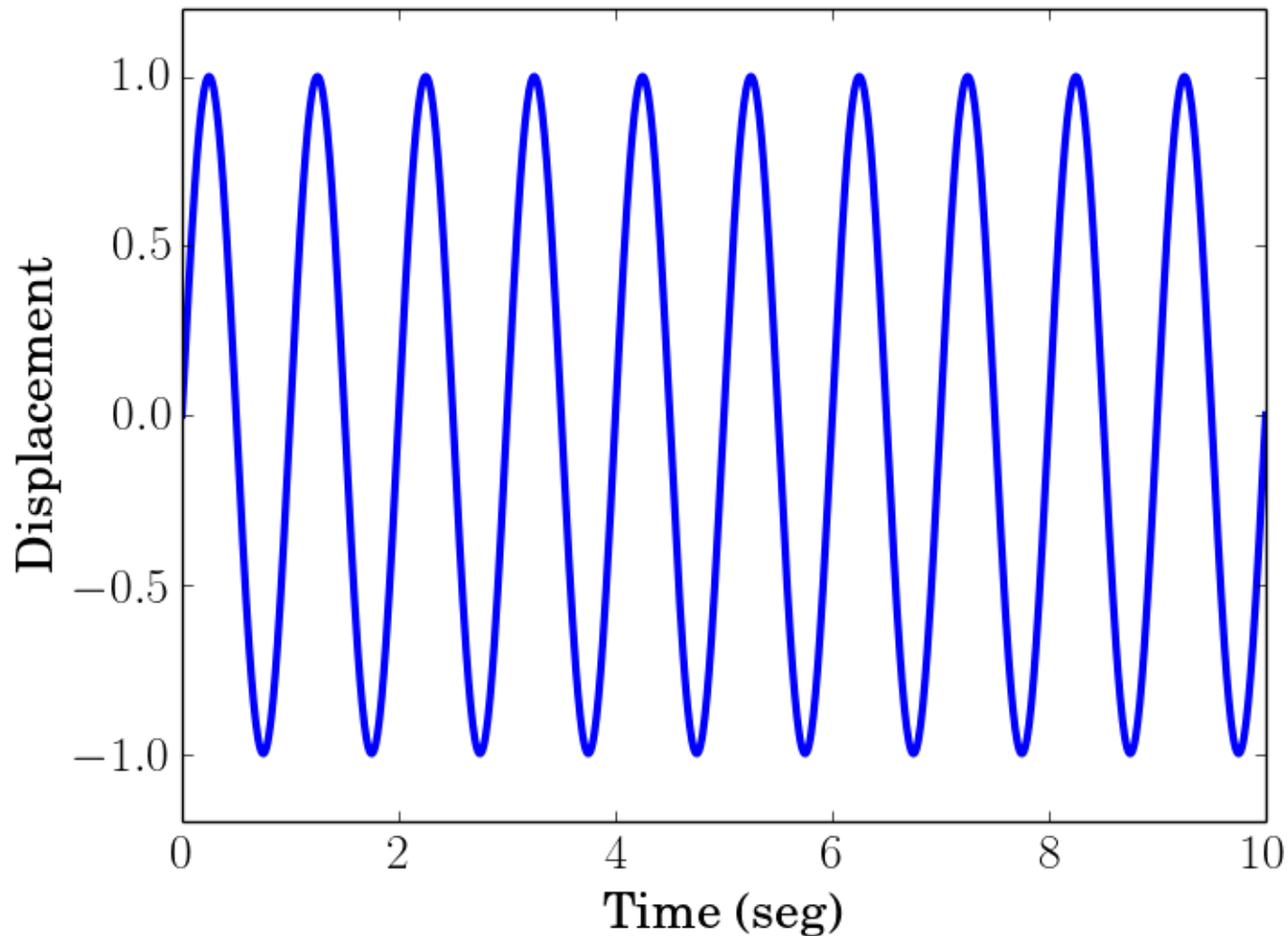
Subscripts  
 $t$  : tire     $v$  : vehicle  
 $w$  : wheel     $r$  : rider  
 $s$  : strut     $eq$  : equivalent



(e)

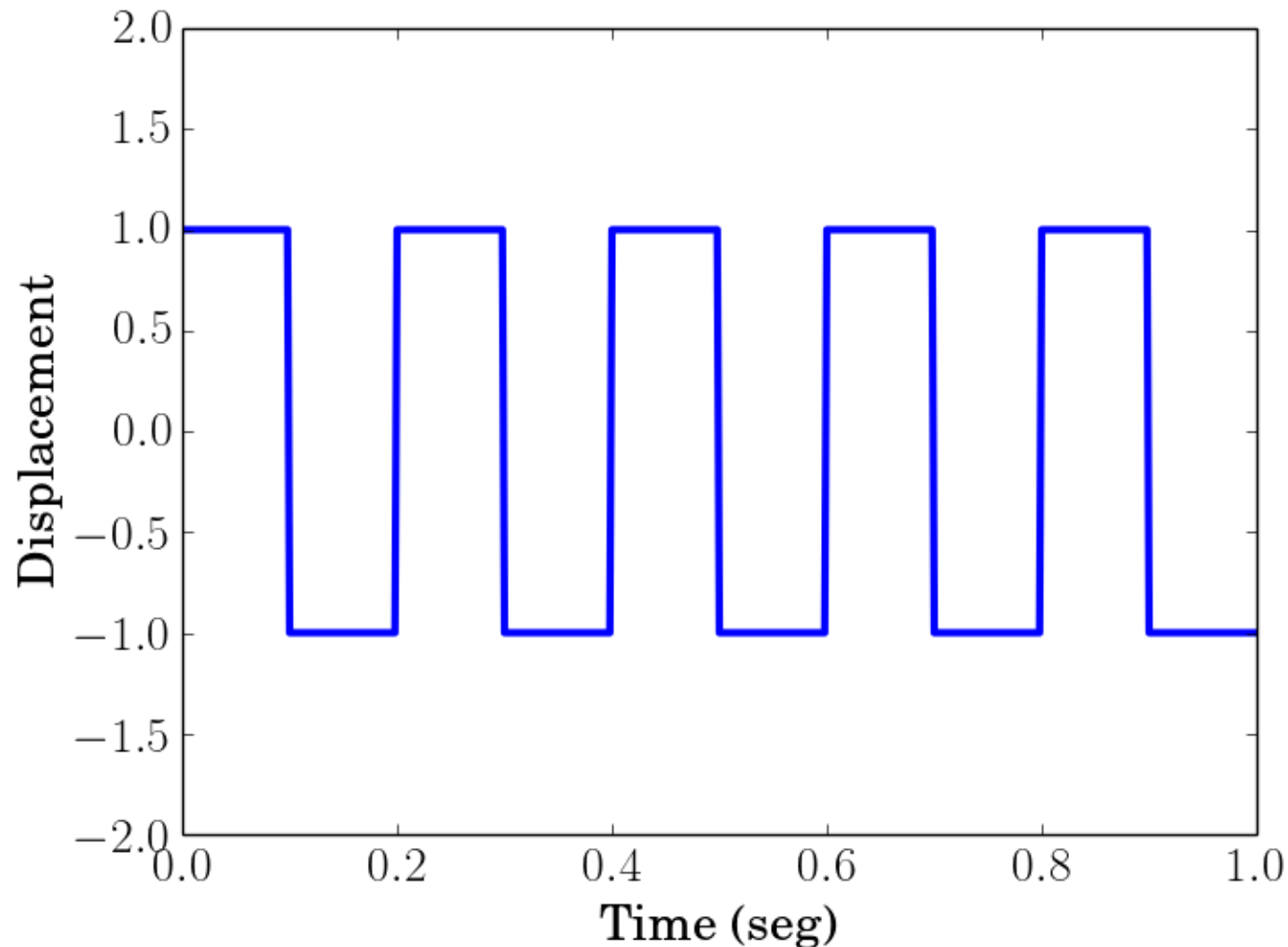
# Types of Vibration Responses

## Periodic Vibration



# Types of Vibration Responses

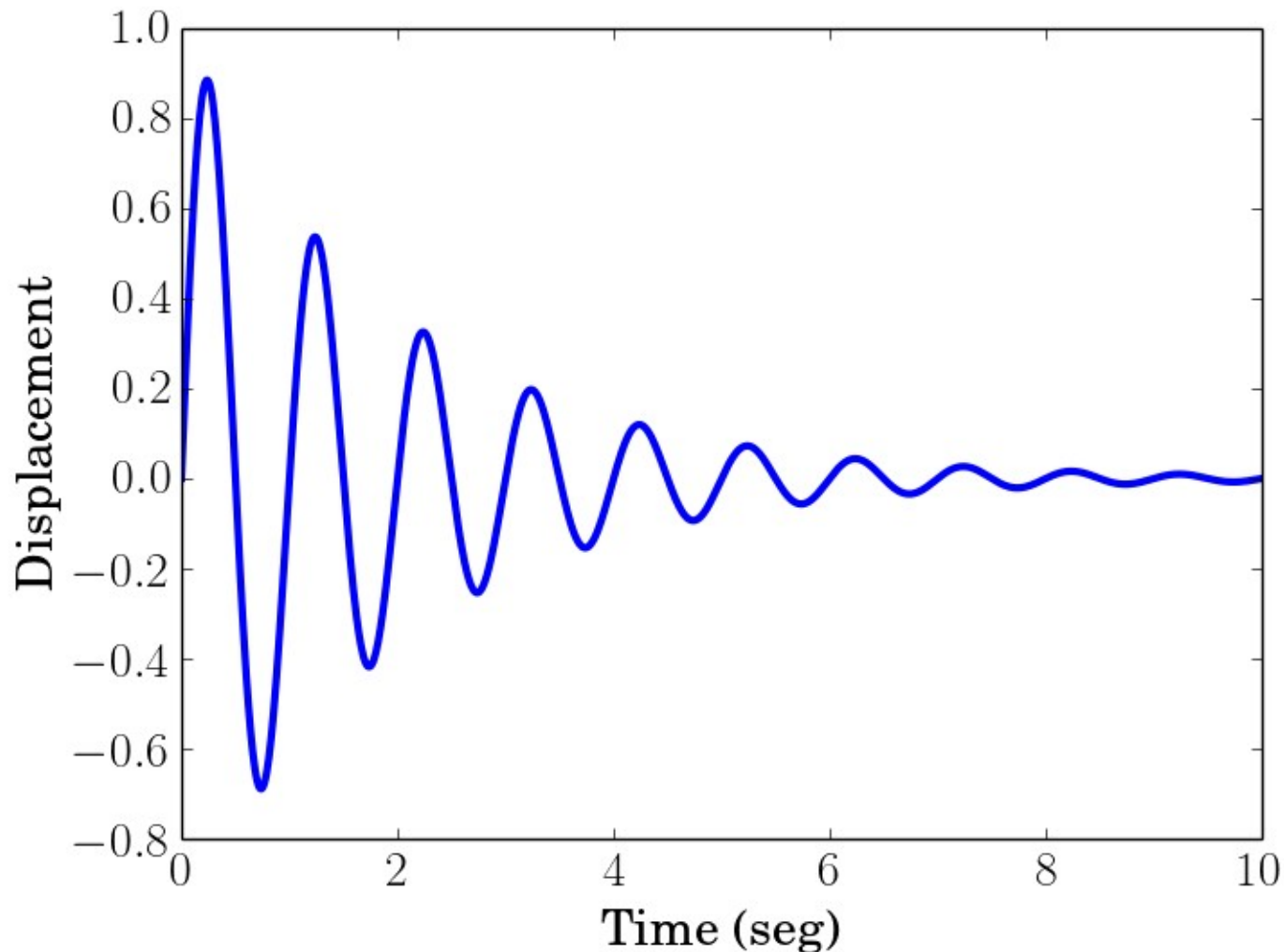
## Periodic Vibration





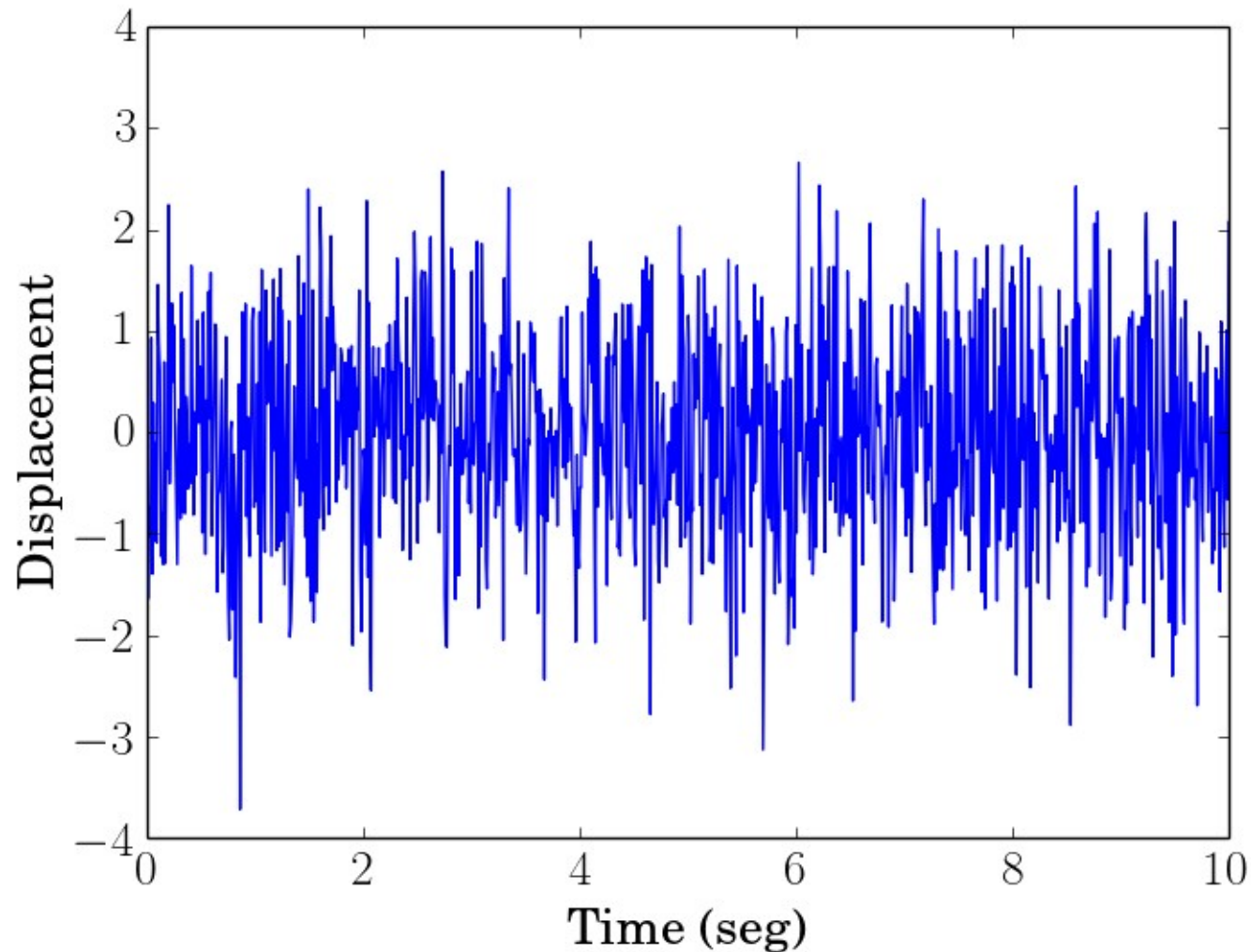
# Types of Vibration Responses

## Transient Vibration



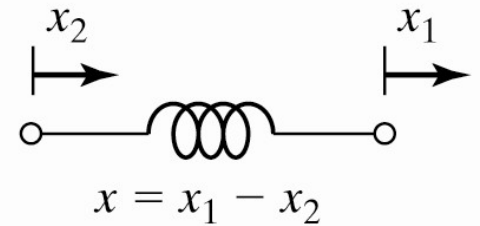
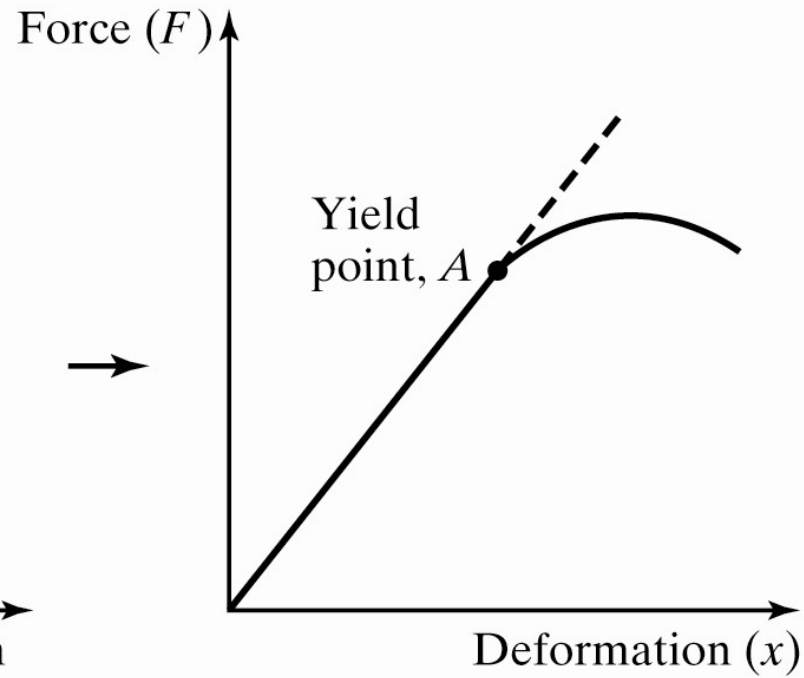
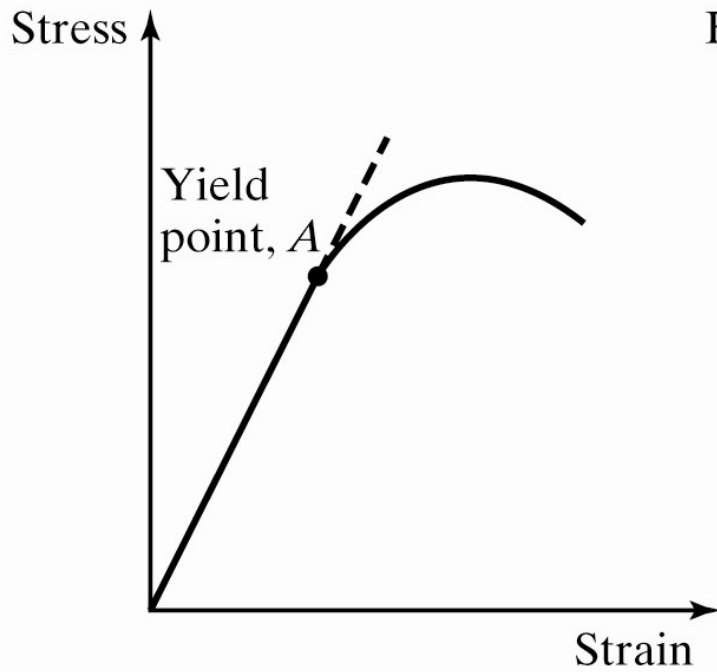
# Types of Vibration Responses

## Random Vibration



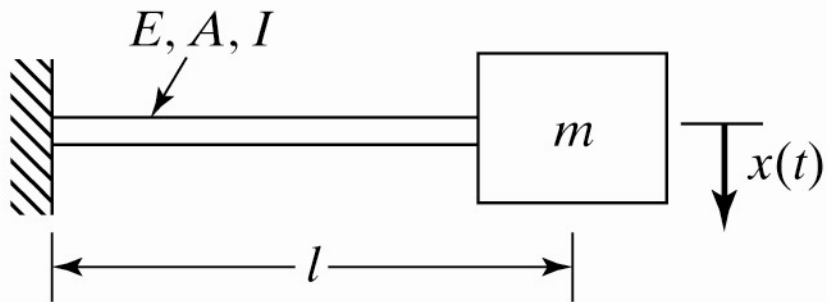
# Basic Concepts

## Stiffness

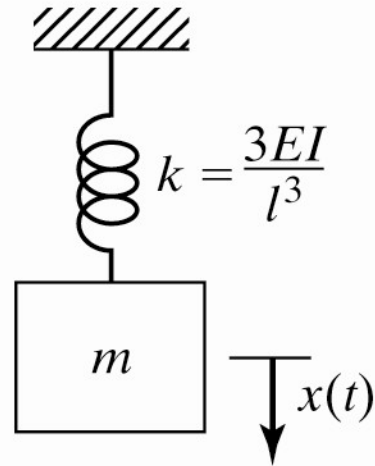


# Basic Concepts

## Stiffness



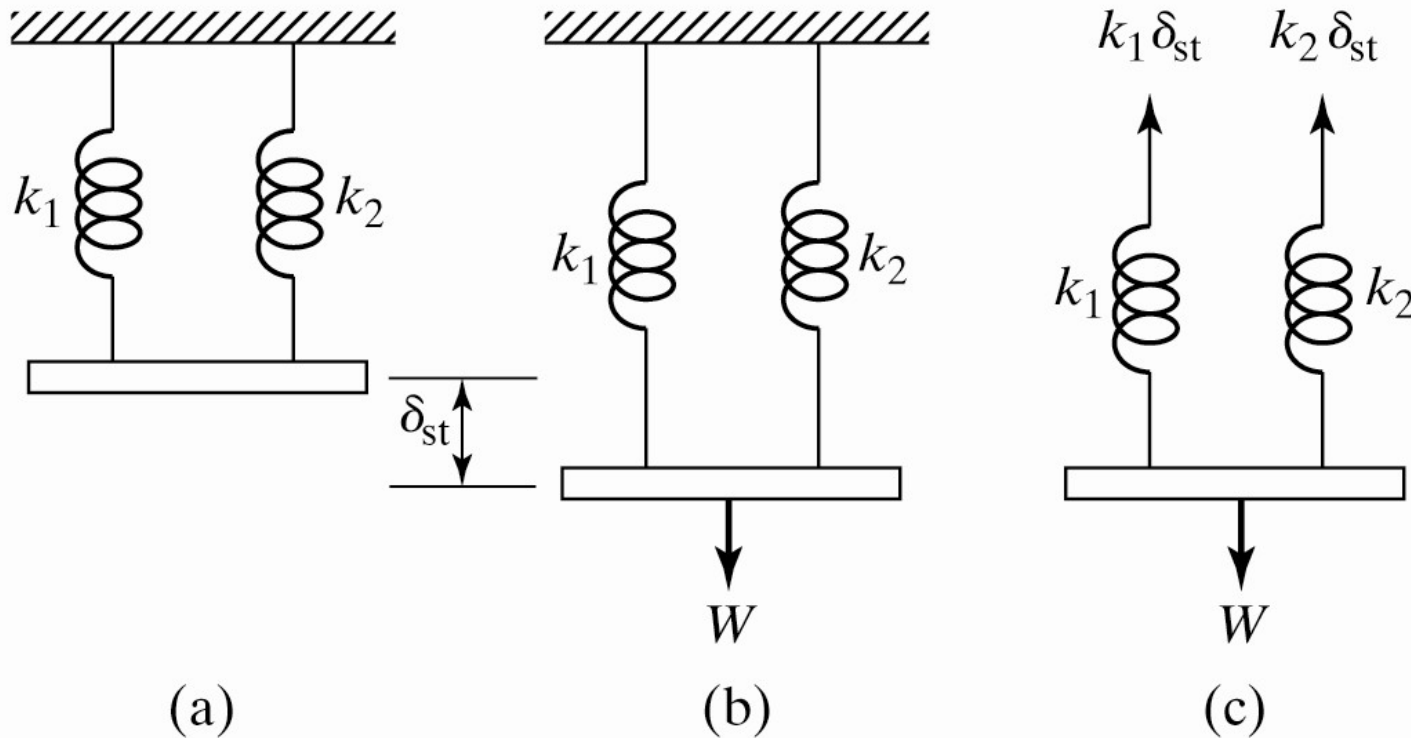
(a) Actual system



(b) Single degree of freedom model

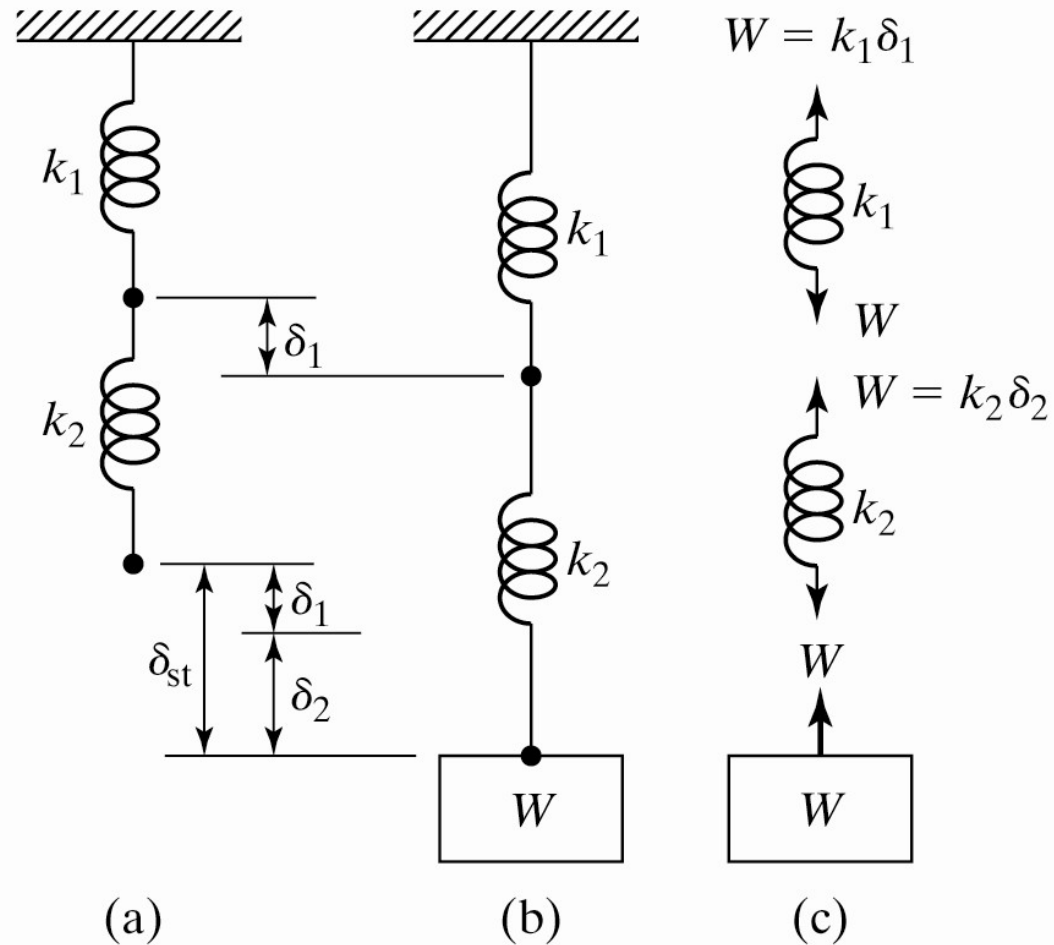
# Basic Concepts

## Stiffness – Parallel arrangement



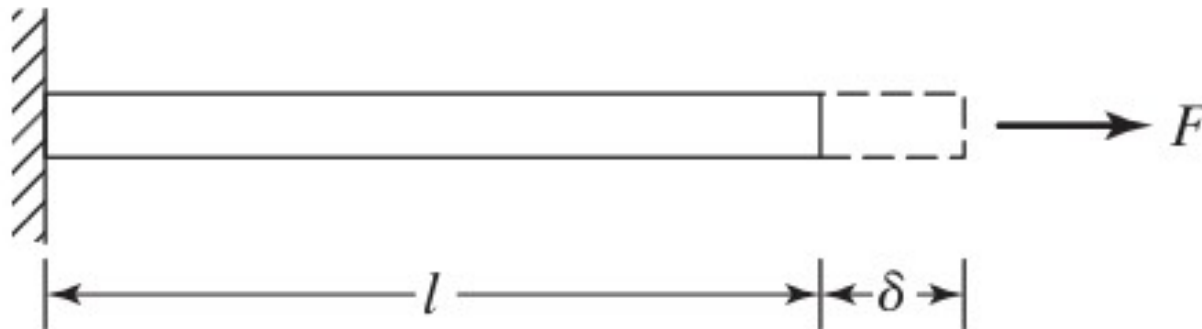
# Basic Concepts

## Stiffness – Series arrangement

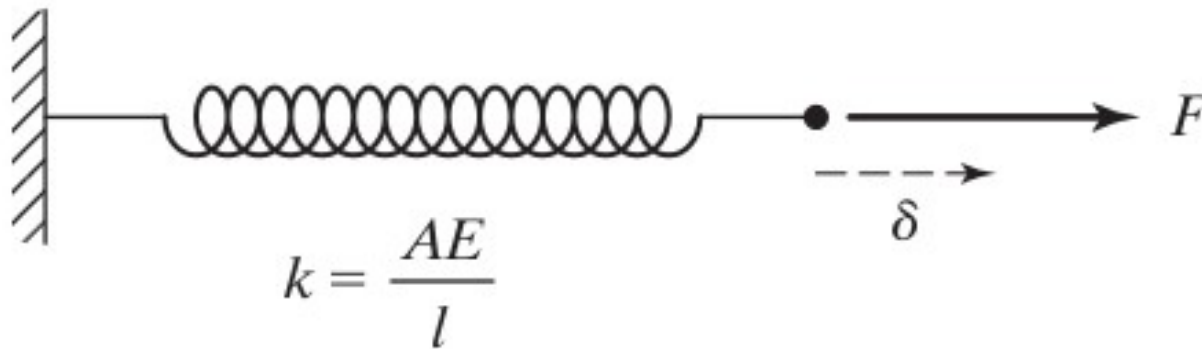




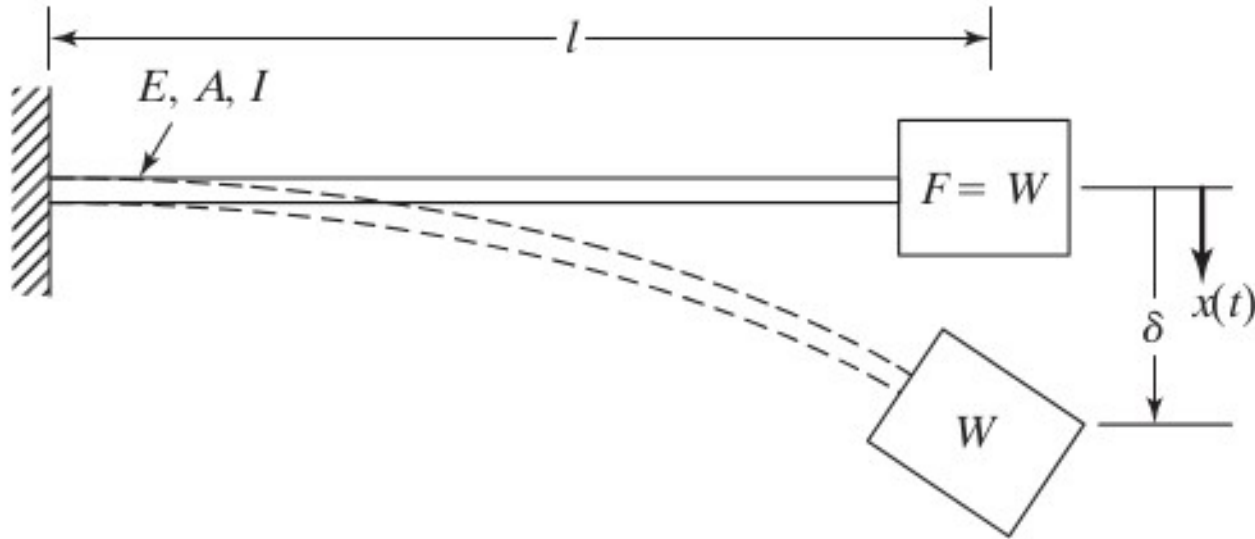
# Equivalent Stiffness



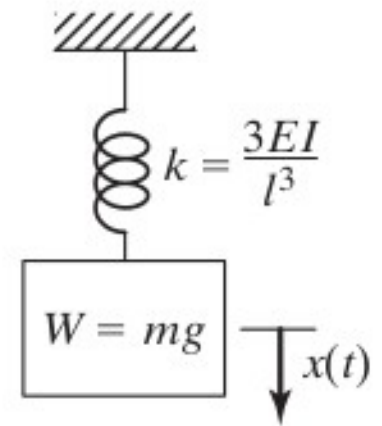
(a)



# Equivalent Stiffness



(a) Cantilever with end force



(b) Equivalent spring

# Equivalent Stiffness

